Phosphomolybdic acid supported atomically dispersed transition metal atoms (M = Fe, Co, Ni, Cu, Ru, Rh, Pd, Ag, Os, Ir, Pt, and Au): stable single atom catalysts studied by density functional theory†

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By means of first-principles calculations, the interaction of twelve different transition metal atoms (M = Fe, Co, Ni, Cu, Ru, Rh, Pd, Ag, Os, Ir, Pt, and Au) of groups VIII–XI with phosphomolybdic acid ($H_3PMo_{12}O_{40}$, PMA), a newly emerging medium for trapping transition metal atoms, has been systematically investigated. The M–PMA systems have very high stability with the binding energies of transition metals higher than those on widely used metal oxide supports. The high diffusion barriers of these single metal atoms on the PMA surfaces suggest that they are sufficiently stable to prevent agglomeration. Based on the electronic structure analysis, the remarkable stability of single atoms is attributed to the strong mixing between the d orbitals of the metal atom and 2p orbitals of PMA oxygens, which results in electron transfer from the metal atoms to PMA, producing positively charged single metal atoms which can be used for catalytic applications. Finally, we test the activity of Pt–PMA as a low-cost, stable, and efficient catalysts for CO oxidation. This work is expected to provide useful insight to the development of new highly efficient heterogeneous single atom catalysts (SACs).

1. Introduction

Single-atom catalysis, in which reactions are catalyzed with extremely high performance efficiencies by metal atoms atomically dispersed on a support, has attracted more and more attention in both experiment and theory.[1–27] The atomic form of the catalyst greatly increases the catalytic efficiency, which could potentially lead to a dramatic reduction of precious metal demands and thus costs. In recent reports, most of the single atoms were anchored onto metal oxides or metal surfaces through various experimental techniques. For example, Zhang' group reported for the first time that isolated single Pt atoms were able to disperse on the surfaces of iron oxide (FeO_x) with excellent stability and exhibit high reaction activity for both CO oxidation and preferential oxidation of CO in H_2.[3] Vilé and the co-workers reported that single Pd atoms anchored to cavities of mesoporous polymeric graphitic carbon nitride can be successfully applied to catalyze hydrogenation of alkynes and

nitroarenes with high activity and product selectivity.[12] More recently, Datye and coworkers demonstrated that isolated single Pd atoms supported by γ-Al_2O_3 had large binding energies and strong catalytic activity for CO oxidation, which is supported by density functional theory (DFT) calculations.[16]

It should be noted, however, that the structures of single atom catalysts (SACs) could undergo significantly changes under some catalytic conditions with high temperatures or pressures, leading to partial or complete loss of the expected reaction activity due to the formation of nanoparticles through agglomeration.[16] Therefore, searching for effective supports that can provide a sufficient concentration of surface sites for trapping transition metal atoms to prevent agglomeration remains a challenge in the design and synthesis of SACs.

Importantly, the catalytic properties of the trapped metal atoms are often different from those of the corresponding bulk metal, because of their strong interactions with the support. Such interactions can be electrostatic in nature, but more common are transfer of charges.[28] In this sense, SACs share some commonalities with homogeneous catalysis, in which the properties of the ligands greatly affect the catalytic properties of the metal center.[5] Ultimately, it would be highly desirable to design SACs by varying the metal interactions with

Recently, phosphomolybdic acid $H_3PMo_{12}O_{40}$ (denoted as PMA) has emerged as an attractive medium to trap transition metal atoms.[14] Zhang *et al.* developed a stable Pt SAC with a high loading of Pt on PMA. PMA has a classical Keggin structure consisting of molybdenum and oxygen atoms with a phosphorus atom located in the center.[29–31] Thanks to the special configuration of PMA, a range of coordination sites containing exposed oxygen atoms exist for metal atoms to be stably anchored. Particularly, a Pt atom has been shown to bind strongly at the four-fold hollow site on PMA in a distorted square-planar geometry and serves as a homogeneous single-atom catalyst for hydrogenation reactions with high selectivity.[14] That work provides a new direction for designing stable heterogeneous SACs by utilizing the advantageous aspects of coordination chemistry and homogeneous catalysis.

Given the fact that isolated Pt atoms can be positioned on PMA with high stability, it is natural to ask whether these coordination sites can also trap other transition metal atoms such as Pd, Au, and Cu, thus generating new SACs. As far as we know, there are few reports about the single atoms supported by PMA,[14] particularly in theory. In order to obtain a deeper understanding of such specific adsorption characteristics and provide fundamental knowledge for designing and synthesizing stable and effective SACs in experiment, the interaction between transition metal atoms (M = Fe, Co, Ni, Cu, Ru, Rh, Pd, Ag, Os, Ir, Pt, and Au) and PMA coordination sites containing different numbers of oxygen atoms are systematically investigated in this work, using DFT. Our calculation results reveal that the hollow sites formed by four oxygen atoms on PMA facilely trap the transition metal atoms. Interestingly, comparison of the adsorption energies of the M species with PMA to the binding energies of the corresponding atoms in metal nanoparticles indicates high stability of the anchored M species against agglomeration. Clear trends in calculated adsorption energies are found for transition metals in different rows and groups of the periodic table, which help to build general rules for the preparation of stable transition metal SACs. Furthermore, it is shown that the oxygens in the binding site significantly modify the characteristic of the trapped metal atom by charge transfer. Finally, potential catalytic applications of M–PMA catalysts are assessed using CO oxidation as an example. This publication is organized as follows. The calculation details are described in Section 2. The results and discussion are presented in Section 3. The conclusions are given in Section 4.

2. Computational details

All spin-polarization calculations were carried out by using the Vienna ab initio simulation package (VASP)[32–34] with the gradient-corrected PW91 exchange–correction functional.[35] For valence electrons, a plane-wave basis set was used with the energy cut-off set to 400 eV and the ionic cores were described with the projector augmented-wave (PAW) method.[36,37] The cubic unit cell contains a classical Keggin configuration consisting of 12 Mo atoms and 40 O atoms with a P atom located in the center. For the structural optimizations, all the atoms were fully relaxed. In order to avoid the interactions between the

complex and its image, the box length was set to 20 Å. Only the Γ-point was used to sample the Brillouin zone.[38] The electron density for the ground-state was converged with a 10^{-4} eV total energy threshold and the geometries were optimized until the maximum force on any ion was less than 0.01 eV Å^{-1}. To explore the oxidation states of the adsorbed transition metals, Bader charge analysis was performed.[39]

The adsorption energy E_{ads} is defined by $E_{ads} = E_{(M–PMA)} - (E_{(M)} + E_{(PMA)})$, where $E_{(M)}$ is the energy of free transition metal atom, $E_{(PMA)}$ the energy of the free PMA support and $E_{(M–PMA)}$ the total energy of the complex. The charge density difference $(\Delta\rho(r))$ plots were obtained by subtracting the charge densities of the separated M $(\rho_M(r))$ and PMA $(\rho_{PMA}(r))$ from the charge density of the M–PMA complex $(\rho_{M+PMA}(r))$ systems as follows: $\Delta\rho(r) = \rho_{M–PMA}(r) - [\rho_{PMA}(r) + \rho_M(r)]$. In order to obtain the energy barrier, the climbing image-nudged elastic band (CI-NEB) method was employed.[40] The highest image along the minimum energy path was denoted as transition state (TS). The energy barrier E_a of each elementary reaction was calculated by the energy difference between the TS and initial state (IS).

3. Results and discussion

In this work, phosphomolybdic acid, PMA $(H_3PMo_{12}O_{40})$ was selected as the support to trap the single metal atoms. The optimized PMA structure is displayed in Fig. 1 and there are several possible coordination sites on the surface of PMA, including a 4-fold hollow site (4-H), two 3-fold hollow sites (3H–O_c and 3H–O_{bri}) and a bridge site (B–O_c–O_{bri}). The corresponding key geometry parameters are listed in Table 1. The
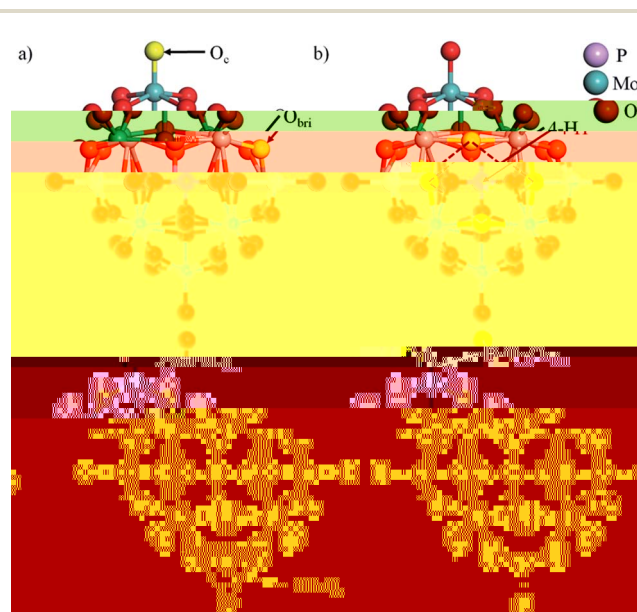

Fig. 1 (a) Optimized PMA with different types of surface O atoms (the corner O atom and bridge O atom are labelled as O_c and O_{bri}) and possible coordination sites (b) 4-fold hollow site (4-H), (c) 3-fold hollow sites (3H–O_c and 3H–O_{bri}) and (d) bridge site (B–O_c–O_{bri}) for metal atoms. The oxygen atoms surrounding the adsorption sites are highlighted in yellow.

Table 1 Calculated P–O, Mo–O_c, Mo–O_{bri}, O_{bri}–O_{bri}(4-H site) bond lengths (Å) in isolated PMA and the comparison with those of previous theories and experiment

Bond	This work	Previous theories[14,31]	Previous experiment[31]
P–O	1.55	1.54, 1.58	1.54
Mo–O_c	1.70	1.69, 1.70	1.68
Mo–O_{bri}	1.94	1.94, 1.94	1.92
O_{bri}–O_{bri}	2.72	—	—

P–O, Mo–O_c and Mo–O_{br} bond lengths are calculated to be 1.55, 1.70 and 1.94 Å, respectively, which are in good agreement with the values from previous experiment and theories.[14,31]

3.1 Geometry and stability of M–PMA

As reported by Zhang *et al.*,[14] Pt atoms can strongly bind at the 4-H sites on PMA. The adsorption energies in Table 2 reveal that PMA can strongly bind not only atomic Pt but other transition metal atoms of groups VIII–XI in the periodic table. Beside the 4-H site, the other sites such as 3H–O_c, 3H–O_{bri} and B–O_c–O_{bri} might also trap the metal atoms. Here, we select one metal from each period (Cu, Ru, and Pt) to systematically investigate all the possible adsorption sites. It can be seen from Fig. 2 that after optimization the metal atoms are located at their initially positioned sites except for Cu and Ru, which migrate from the initial 3H–O_c site to 4-H. Not surprisingly, the calculated adsorption energies (see Table S1†) indicate that the most stable site for all metal atoms is the 4-H site. For Cu, the adsorption energy becomes stronger in the order B–O_c–O_{bri} < 3H–O_{bri} < 4-H with the values of −4.49, −5.02 and −7.50 eV, respectively. The calculated bond lengths for Cu–O are around 1.90 Å. For Ru, the binding energy at 3H–O_{bri} is almost equal to
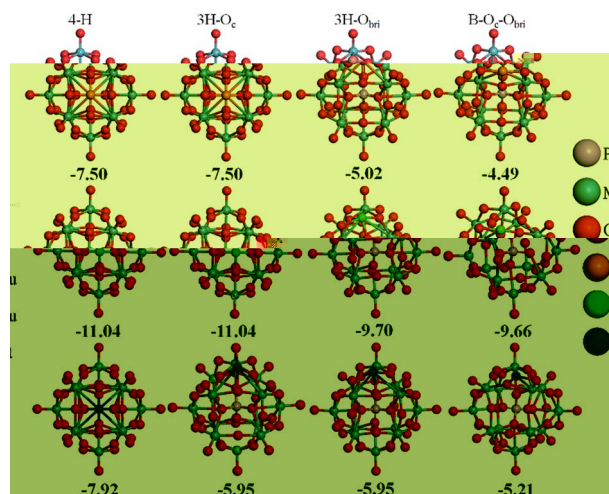

Fig. 2 Optimized configurations of M−PMA (M = Cu, Ru and Pt) with M initially positioned at the 4-H, 3H−O_c (note that for Cu and Ru, the atoms fall back to 4H), 3H−O_{bri}, and B−O_c−O_{bri} sites (from left to right), respectively. The metal atoms are represented with different colors.

that at B–O_c–O_{bri} with a value of −9.66 eV. At the 3H–O_{bri} site, the calculated Ru–O bond lengths are 1.89, 1.89 and 2.09 Å, respectively; and at the bridge site the values are 1.71 and 1.82 Å. For Pt, the largest binding energy is −7.92 eV at the 4-H site. This atom can be also stable at the 3H–O_c site with an adsorption energy of −5.95 eV and the site of B–O_c–O_{bri} possesses the smallest binding energy of −5.21 eV. In this case, the average Pt–O bond distance is calculated to be about 1.89 Å. Based on the calculation results, it can be concluded that the most stable adsorption site for these three transition atoms is the 4-H site surrounded by four bridge oxygen atoms, which is consistent

Table 2 Calculated M−O and O−O distances (d/Å), ∠O−M−O (°), adsorption energy (E_{ads}/eV), and Bader charge (q/|e|) for M at the anchoring sites of the M−PMA systems. Only the oxygen atoms surrounding M are taken into account

M	d_{M-O}	d_{O-O}	∠OMO	E_{ads}	E_{coh}[20]	q
Group VIII						
Fe	1.81, 1.81, 1.84, 1.84	2.55, 2.55, 2.55, 2.55	88.6, 88.6, 88.6, 88.6	−10.90	−4.28	1.42
Ru	1.90, 1.90, 2.03, 2.03	2.55, 2.60, 2.55, 2.60	80.8, 82.8, 82.8, 80.9	−11.04	−6.74	1.34
Os	1.88, 1.86, 1.96, 2.01	2.46, 2.56, 2.46, 3.12	79.5, 82.2, 109.6,78.8	−11.24	−8.17	1.42
Group IX						
Co	1.81, 1.81, 1.83, 1.83	2.53, 2.53, 2.53, 2.53	87.9, 87.9, 87.9, 87.9	−10.41	−4.39	1.26
Rh	1.88, 1.88, 2.08, 2.08	2.61, 2.61, 2.61, 2.61	82.3, 82.3, 82.3, 82.3	−9.11	−5.74	1.11
Ir	1.86, 1.85, 2.06, 2.04	2.52, 3.10, 2.51, 2.65	80.1, 105.4, 85.3, 80.2	−10.08	−6.94	1.21
Group X						
Ni	1.78, 1.78, 1.87, 1.87	2.55, 2.55, 2.55, 2.55	88.6, 88.6, 88.6, 88.6	−9.35	−4.44	1.18
Pd	1.94, 1.94, 2.04, 2.04	2.71, 2.71, 2.71, 2.71	85.7, 85.7, 85.7, 85.7	−6.44	−3.90	1.03
Pt	1.94, 1.94, 2.04, 2.04	2.75, 2.75, 2.75, 2.75	87.3, 87.5, 87.5, 87.4	−7.92	−5.85	1.05
Group XI						
Cu	1.82, 1.82, 1.84, 1.84	2.57, 2.57, 2.57, 2.57	89.3, 89.3, 89.3, 89.3	−7.50	−3.48	1.18
Ag	2.01, 2.01, 2.02, 2.02	2.77, 2.77, 2.77, 2.77	86.9, 86.9, 86.9, 86.9	−4.63	−2.94	1.06
Au	2.00, 2.00, 2.02, 2.02	2.80, 2.80, 2.80, 2.80	88.2, 88.2, 88.2, 88.2	−5.04	−3.81	1.03

with the DFT results of the Pt–PMA system reported by Zhang *et al.*[14] In the following sections, only the 4-H site is considered for all transition metals examined.

We also explore whether PMA can still trap transition metal atoms strongly enough with a high loading of metal atoms, since each PMA contains more than one 4-H site. From the calculated results (the configurations and adsorption energies are shown in Fig. S1 and Table S2 in ESI,† respectively), it is found that the adsorption energies for the second and third metal atoms at 4-H sites are somewhat smaller than the those for the first one: −6.14 and −5.23 eV for Pt, −9.49 and −8.56 eV for Ru, −5.11 and −4.36 eV for Cu, respectively. These results suggest that it might be possible to have multiple metal atoms trapped in different sites of a single PMA, further increasing the SAC concentration.

The top views of the optimized structures for the M–PMA systems with a single trapped M are displayed in Fig. 3. It is shown from the side view that all the metal atoms are located at 4-H sites and protrude slightly from the oxygen plane after structural relaxation. As shown in Table 2, the calculated d_{M-O} and d_{O-O} distances of M–PMA reveal that the coordination type is approximately symmetric, except for the cases of Os and Ir. For example, the d_{Fe-O} distances are 1.81, 1.81, 1.84 and 1.84 Å and the d_{O-O} distances are all equal to 2.55 Å. The square-planar configurations are significantly distorted for both Os and Ir as the d_{O-O} distances are substantially changed from the initial values of 2.72 Å to 2.46, 2.56, 2.46 and 3.12 Å for Os and 2.52,

3.10, 2.51 and 2.65 Å for Ir, respectively, probably due to their large atomic radii. In addition, the d_{Os-O} values are calculated to be 1.88, 1.86, 1.96 and 2.01 Å and the d_{Ir-O} values are 1.86, 1.85, 2.06 and 2.04 Å.

Next we look into the stabilization of the trapped metal atoms on PMA. In group VIII, with the increasing of atomic radius in the order of Fe < Ru < Os, their adsorption energies rank in the following descending order: Os > Ru > Fe. However, it is noted that the adsorption energies are quite similar around −11 eV, indicating that these trapped atoms are very stable on PMA. These adsorption energies are comparable to those on the $CeO_2(100)$ surface,[20] a widely used substrate for trapping single atoms. On $CeO_2(100)$, an M atom at the surface Ce^{4+} vacancy interacts with four lattice oxygen atoms, generating a square-planar configuration, similar to that in M–PMA complexes. For metals in group IX, the Co atom in PMA has the largest binding energy of −10.41 eV. On the other hand, the Rh atom has the smallest binding energy of −9.11 eV, but is still about 2 eV higher than that on CeO_2 (−7.03 eV) and Fe_2O_3 (−7.34 eV).[20,23] For group X metals, the interaction between the transition metal atom and PMA support becomes weaker and the binding energy becomes stronger in the order: Pd (−6.44 eV) < Pt (−7.92 eV) < Ni (−9.35 eV). For comparison, these values for Pd and Pt are also a little bit larger than those on CeO_2 (−5.22 and −7.02 eV) and FeO_x (−5.62 and −6.67 eV),[20,23] revealing the ability of PMA to strongly bind these metal atoms. For group XI, in general, the binding energies of Cu, Ag and Au are much weaker when compared with those of other metals. The smallest binding energy is found for Ag with a value of −4.63 eV, however, still higher than that on the CeO_2 support (−2.87 eV).[20]

As displayed in Fig. 4, clear trends in the calculated E_{ads} can also be seen along the periods and groups of the periodic table. From the left to the right of a period, E_{ads} is reduced in magnitude, which is attributed to the more occupied d orbitals of metals forming weaker bonds with the oxygens of PMA. For 4d metals, the trend for E_{ads} is monotonous from Ru to Ag. While the trend along the period for 3d and 5d metals becomes less monotonic. In general, these trends reveal that the single atoms of 4d metals yield the weakest bonds with the oxygen
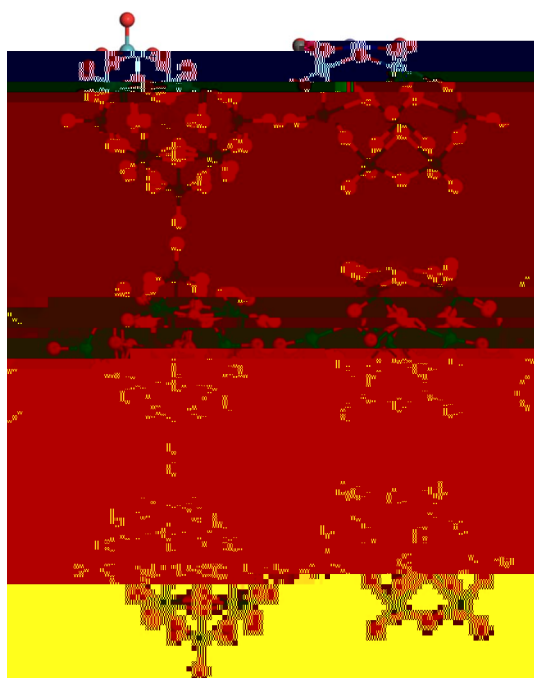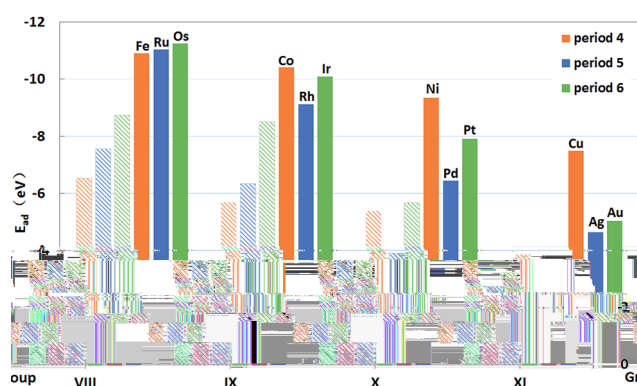

Fig. 3 Top and side view of the optimized configurations of the M–PMA (M = Fe, Os, and Ir) systems (the configurations of other M–PMAs are close to that of symmetric Fe–PMA and thus not shown here). The metal atoms are represented with different colors, the oxygen atoms surrounding the adsorption sites (4-H) are highlighted in yellow and the calculated distances of the M–O bonds are listed in Table 2.

Fig. 4 Binding energies (filled columns) of single transition metal atoms (M) trapped on PMA and binding energies[20] (shadowy columns) of these atoms in edge positions of the M_{79} nanoparticles of the same atoms.

atoms at the 4-H sites, quite similar to that on CeO_2.[20] However, the 3d metals can interact with the oxygen atoms by forming the strongest bonds with the exception of Fe, contrast to that on CeO_2 where 5d metals have largest binding energies.[20] As shown in Table 2, the lengths of M–O bonds are less than 1.90 Å, which are shorter than those for 4d and 5d metals. That may be due to the fact that atom radii of 3d atoms are smaller than those of 4d and 5d atoms. This comparison underscores the fact that the trends for the adsorption energy of single metal atoms depend on the selected support. In Fig. 4, the adsorption energies of M on PMA are also compared with those for these atoms in edge positions of the M_{79}
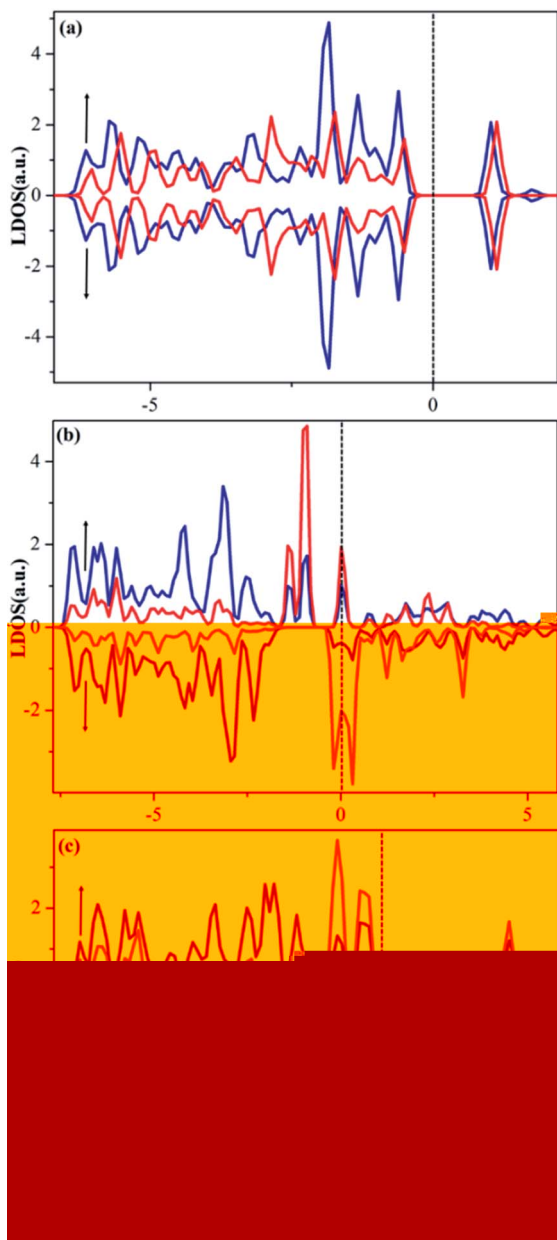
Fig. 6 Spin-polarized LDOSs projected on 2p orbitals (blue) of O and d orbitals (red) of Cu (a), Ru (b) and Pt (c) embedded in the 4-H site of PMA. The Fermi level was set to zero.
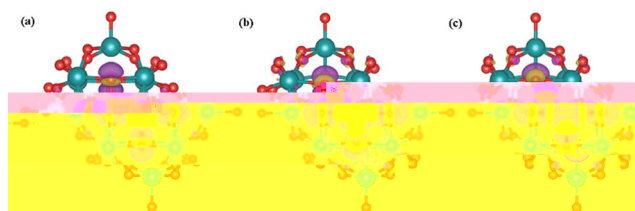
observed. However, it is believed there is a net depletion in each metal atom, which has been already revealed by the Bader charge calculations that metal atoms are positively charged. For example, it is known that positively charged Pt captures hydrogen easily and exhibits excellent activity in the hydrogenation of nitrobenzene and cyclohexanone.[14] In our previous study, it was found that the defected h-BN supported metal atoms such as Fe, Co, Cu and Pt possess positive charges with a range of +0.64–1.02|e|, which are responsible to the predicted high activity of CO oxidation.[17,19]

3.3 Model CO oxidation

To test the ability of M–PMA SACs, we have computed the reaction energetics for CO oxidation, a prototypical catalysis reaction. The activation of oxygen molecules was investigated first since it is an important step of CO oxidation.[3,16,17] The calculated O–O bond of the O_2 adsorbed on the metal center of M–PMA is found to be elongated, suggesting O_2 activation. For example, as shown in Fig. S2,† the O–O bond length on Ru–PMA is significantly elongated from its equilibrium value of 1.23 Å to 1.36 Å, yielding a binding energy of −1.37 eV for the adsorbed O_2 species. While for a non-precious metal such as Fe, the O_2 molecule has an adsorption energy of −0.48 eV with the length of the O–O bond changed to 1.33 Å, implying efficient activation of O_2 on Fe–PMA. In addition, the reaction of $CO + O_2 \rightarrow CO_2 + O$ is investigated on Pt–PMA. As shown in Fig. 8, in IS the CO molecule is co-adsorbed with O_2 in which the O–O bond length is about 1.27 Å. At the transition state, the O–O bond distance is further elongated to 1.37 Å and the carbon atom of CO connects to one of oxygen atoms in O_2 with a bond length of 1.69 Å. This reaction step for the production of a CO_2 molecule requires to overcome an energy barrier of 0.59 eV, which is much lower than those (around 1 eV) on transition metal surfaces such as Pt, Au and Ag.[41–43] In addition, this reaction is quite exothermic with ΔE equal to −1.01 eV. For the reaction between the second CO and the remaining O atom ($CO + O \rightarrow CO_2$), the calculated

Fig. 7 Contour plots of differential charge density of Cu (a), Ru (b) and Pt (c) adsorption on PMA. The charge accumulation regions are rendered in purple, and the charge depletion region in yellow (the isovalue is ±0.003 au).
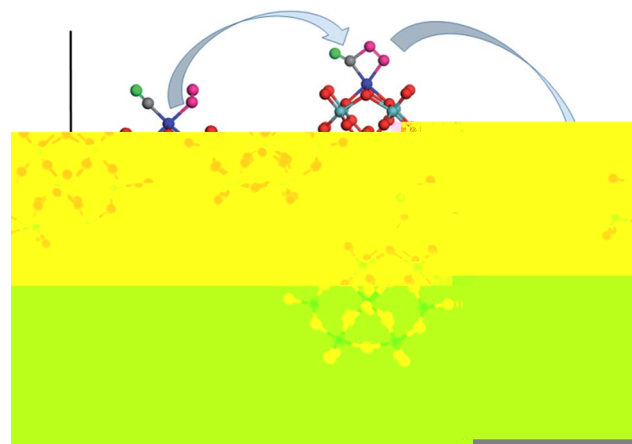

Fig. 8 Calculated energetics and structures for IS, TS and FS of $CO + O_2 \rightarrow CO_2 + O$ on Pt–PMA. To avoid confusion, the colors for the O atoms in O_2 molecule, the O atom in CO molecule and C atom are represented in pink, green and grey, respectively.

energy barrier is also quite small (0.22 eV) and the exothermicity is found to be −2.14 eV. In order to find out whether the other supported metal atoms have catalytic activity, we also investigated CO oxidation on PMA supported single Ru atom. The energy barrier for the reaction ($CO + O_2 \rightarrow CO_2 + O$) is about 0.75 eV with a large exothermicity of −3.13 eV, suggesting its strong activity. For Ru–PMA, the $CO + O \rightarrow CO_2$ step overcomes an energy barrier as high as 0.95 eV, which is much larger than that (0.22 eV) on Pt–PMA. It can be attributed to the fact that the oxygen atom is strongly bounded to the Ru–PMA complex with a binding energy of −3.36 eV, about 3 eV larger than that on Pt–PMA. Our calculation results indicate that the adsorption energy of the intermediate species such as an oxygen atom plays an important role in the oxidation process. If this value is found to be large, the oxygen species might not be facilely taken away by the second CO molecule and the catalyst might be poisoned. Overall, our results suggest that Pt–PMA can efficiently catalyse this prototypical process. Further calculations of CO oxidation on other M–PMA SACs will be reported in another paper.

4. Conclusions

In this work, single transition metal atoms (M = Fe, Co, Ni, Cu, Ru, Rh, Pd, Ag, Os, Ir, Pt, and Au) embedded in phosphomolybdic acid were systematically explored by using a DFT method in an effort to gain insights into the metal binding and catalytic potentials. From the calculation results, we found such systems are very stable with each single metal atom coordinated by four oxygen atoms at the 4-H site in a distorted square-planar configuration and slightly protrudes from the oxygen planar surface. The adsorption energ20.9(y)-

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